

# Chapter 13 Drill

The answers and explanations can be found in Chapter 17.

## Section I: Multiple Choice

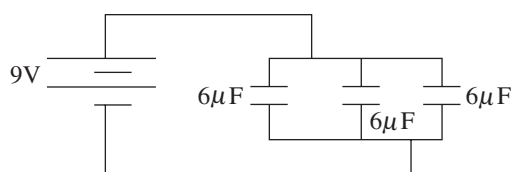
1. A capacitor is fully charged by a battery. The battery is disconnected, and a dielectric is inserted into the capacitor. Which of the following statements is/are true?

- I. The voltage will remain the same.
- II. The potential energy of the capacitor will increase.
- III. The capacitance of the capacitor will increase.

- (A) I only
- (B) I and II only
- (C) I and III only
- (D) II and III only
- (E) III only

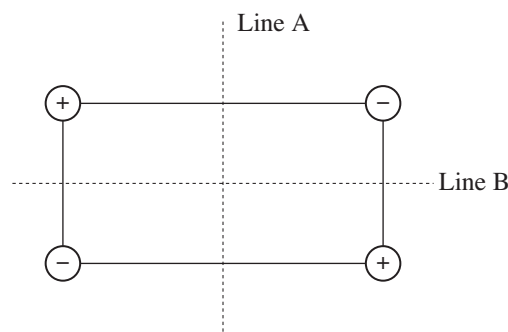
2. If the electric field does negative work on a negative charge as the charge undergoes a displacement from Position A to Position B within an electric field, then the electrical potential energy

- (A) is negative
- (B) is positive
- (C) increases
- (D) decreases
- (E) cannot be determined from the information given



3. Three  $6\ \mu\text{F}$  capacitors are connected in parallel to a  $9\ \text{V}$  battery as shown above. Determine the energy stored in each capacitor.

- (A)  $243\ \text{J}$
- (B)  $7.29 \times 10^{-4}\ \text{J}$
- (C)  $8.10 \times 10^{-5}\ \text{J}$
- (D)  $2.43 \times 10^{-4}\ \text{J}$
- (E)  $27\ \text{J}$

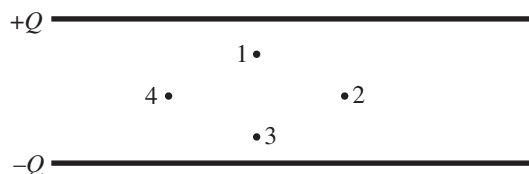


4. The picture above shows 4 charges fixed in position at the corners of a rectangle measuring  $2\ \text{cm}$  by  $4\ \text{cm}$ . Assuming the charges are all of equal magnitude, how many locations on either Line A or Line B would be places with 0 net electric potential?

- (A) 1
- (B) 5
- (C) All of Line A
- (D) All of Line B
- (E) All of both Line A and Line B

5. A particle with a charge of  $+q$  and mass  $m$  starts at rest and moves linearly from a position of high potential,  $A$ , to a position of low potential,  $B$ . Which of the following expressions will give the particle's speed at position  $B$ ?

- (A)  $\sqrt{\frac{2q(V_A - V_B)}{m}}$
- (B)  $\sqrt{\frac{2q(V_B - V_A)}{m}}$
- (C)  $\sqrt{\frac{q(V_A - V_B)}{m}}$
- (D)  $\sqrt{\frac{q(V_A - V_B)}{2m}}$
- (E)  $\sqrt{\frac{2q(V_B - V_A)}{2m}}$



6. Which points in this uniform electric field (between the plates of the capacitor) shown above lie on the same equipotential?

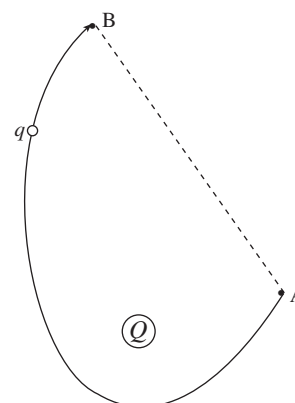
- (A) 1 and 2 only
- (B) 1 and 3 only
- (C) 2 and 4 only
- (D) 3 and 4 only
- (E) 1, 2, 3, and 4 all lie on the same equipotential since the electric field is uniform.

7. Two isolated and widely separated conducting spheres each carry a charge of  $-Q$ . Sphere 1 has a radius of  $a$  and Sphere 2 has a radius of  $4a$ . If the spheres are now connected by a conducting wire, what will be the final charge on each sphere?

	Sphere 1	Sphere 2
(A)	$-Q$	$-Q$
(B)	$-2Q/3$	$-4Q/3$
(C)	$-4Q/3$	$-2Q/3$
(D)	$-2Q/5$	$-8Q/5$
(E)	$-8Q/5$	$-2Q/5$

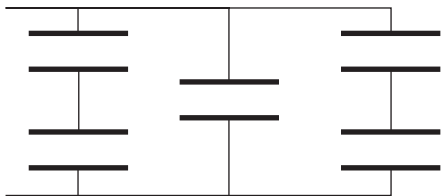
8. A parallel-plate capacitor is charged to a potential difference of  $\Delta V$ ; this results in a charge of  $+Q$  on one plate and a charge of  $-Q$  on the other. The capacitor is disconnected from the charging source, and a dielectric is then inserted. What happens to the potential difference and the stored electrical potential energy?

- (A) The potential difference decreases, and the stored electrical potential energy decreases.
- (B) The potential difference decreases, and the stored electrical potential energy increases.
- (C) The potential difference increases, and the stored electrical potential energy decreases.
- (D) The potential difference increases, and the stored electrical potential energy increases.
- (E) The potential difference decreases, and the stored electrical potential energy remains unchanged.



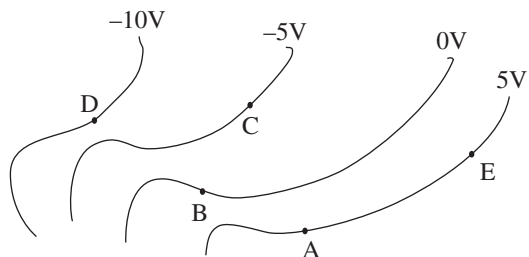
9. How much work would the electric field (created by the stationary charge  $Q$ ) perform as a charge  $q$  is moved from Point A to B along the curved path shown?  $V_A = 200$  V,  $V_B = 100$  V,  $q = -0.05$  C, length of line segment AB = 10 cm, length of curved path = 20 cm.

- (A)  $-10$  J
- (B)  $-5$  J
- (C)  $+5$  J
- (D)  $+10$  J
- (E)  $+2$  J



10. If each of the capacitors in the array shown above is  $C$ , what is the capacitance of the entire combination?

(A)  $C/2$   
 (B)  $2C/3$   
 (C)  $5C/6$   
 (D)  $2C$   
 (E)  $5C/3$

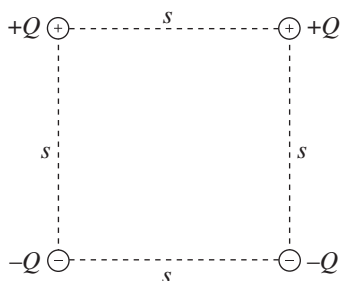


11. The diagram above shows equipotential lines produced by a charge distribution.  $A$ ,  $B$ ,  $C$ ,  $D$ , and  $E$  are points in the plane. An electron begins at point  $A$ . The electron is then moved to point  $E$  and then from point  $E$  to point  $C$ . Which of the following correctly describes the work done *by the field* for each part of the movement?

	Movement from $A$ to $E$	Movement from $E$ to $C$
(A)	Negative	Positive
(B)	Zero	Positive
(C)	Zero	Negative
(D)	Negative	Zero
(E)	Positive	Positive

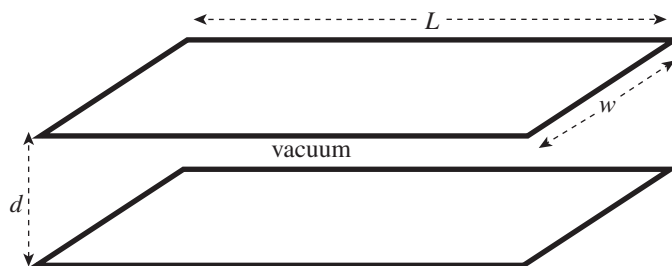
## Section II: Free Response

1. In the figure shown, all four charges are situated at the corners of a square with sides  $s$ .



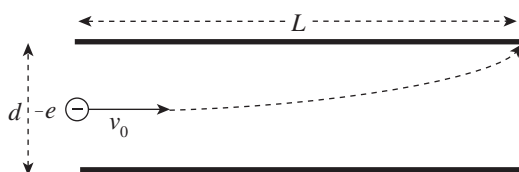
- (a) What is the total electrical potential energy of this array of fixed charges?
- (b) What is the electric field at the center of the square?
- (c) What is the electric potential at the center of the square?
- (d) Sketch (on the diagram) the portion of the equipotential surface that lies in the plane of the figure and passes through the center of the square.
- (e) How much work would the electric field perform on a charge  $q$  as it moved from the midpoint of the right side of the square to the midpoint of the top of the square?

2. The figure below shows a parallel-plate capacitor. Each rectangular plate has length  $L$  and width  $w$ , and the plates are separated by a distance  $d$ .



- (a) Determine the capacitance.

An electron (mass  $m$ , charge  $-e$ ) is shot horizontally into the empty space between the plates, midway between them, with an initial velocity of magnitude  $v_0$ . The electron just barely misses hitting the end of the top plate as it exits. (Ignore gravity.)



- (b) In the diagram, sketch the electric field vector at the position of the electron when it has traveled a horizontal distance of  $L/2$ .
- (c) In the diagram, sketch the electric force vector on the electron at the same position as in part (b).
- (d) Determine the strength of the electric field between the plates. Write your answer in terms of  $L$ ,  $d$ ,  $m$ ,  $e$ , and  $v_0$ .
- (e) Determine the charge on the top plate.
- (f) How much potential energy is stored in the capacitor?

3. A solid conducting sphere of radius  $a$  carries an excess charge of  $Q$ .

- (a) Determine the electric field magnitude,  $E(r)$ , as a function of  $r$ , the distance from the sphere's center.
- (b) Determine the potential,  $V(r)$ , as a function of  $r$ . Take the zero of potential at  $r = \infty$ .
- (c) On the diagrams below, sketch  $E(r)$  and  $V(r)$ . (Cover at least the range  $0 < r < 2a$ .)



4. A solid, nonconducting sphere of radius  $a$  has a volume charge density given by the equation  $\rho(r) = \rho_0(r/a)^3$ , where  $r$  is the distance from the sphere's center.
- (a) Determine the electric field magnitude,  $E(r)$ , as a function of  $r$ .
  - (b) Determine the potential,  $V(r)$ , as a function of  $r$ . Take the zero of potential at  $r = \infty$ .
  - (c) On the diagrams below, sketch  $E(r)$  and  $V(r)$ . Be sure to indicate on the vertical axis in each plot the value at  $r = a$ .

